

## SIMPLE INTEREST

### It Really Is Simple

#### CALCULATING SIMPLE INTEREST

Simple interest is calculated as a percentage of the principal on an investment or loan using the formula  $I = Prt$  where:

$$I = \text{Interest amount (accumulated over time)}$$

$$P = \text{Principal (the original amount)}$$

$$r = \text{interest rate (expressed as a decimal)}$$

$$t = \text{length of time (expressed in terms of years)}$$

Simple interest is added to the principal at the end of the period using the formula  $A = P + I$ , where

$$A = \text{Total amount (principal + interest)}$$

#### Interest Rate (r)

Show the following interest rates as they would appear in the simple interest formula as  $r$ .

(Hint: Divide by 100, or move decimal 2 spaces to the left)

$$\text{a) } 13\% = 13 \div 100 = 0.13$$

$$\text{b) } 2.5\% = 2.5 \div 100 = 0.025$$

$$\text{c) } 0.5\% = 0.5 \div 100 = 0.005$$

#### Time (t)

Express the following lengths of time in terms of years ( $t$  in the simple interest formula)

$$\text{a) } 24 \text{ months}$$

$$\text{b) } 8 \text{ months}$$

$$\text{c) } 14 \text{ weeks}$$

$$\text{d) } 82 \text{ days}$$

$$\frac{24}{12} = 2 \text{ years}$$

$$\frac{8}{12} = 0.67 \text{ years}$$

$$\frac{14}{52} = 0.27 \text{ years}$$

$$\frac{82}{365} = 0.22 \text{ years}$$

In the simple interest formula, time **MUST** be expressed in terms of years.

So... if **time** is given in:

- Months → ÷ by 12
- Weeks → ÷ by 52
- Days → ÷ by 365

**EXAMPLE 1**

a) Calculate how much interest is earned if \$2 000 is invested at 4.5% simple interest for 26 weeks.

$$I = ?$$

$$P = \$2000$$

$$r = 4.5\% = 0.045$$

$$t = \frac{26 \text{ weeks}}{52} = 0.5$$

$$I = P \cdot r \cdot t$$

$$= 2000 \cdot 0.045 \cdot 0.5$$

$$= 45$$

∴ The amount of interest earned is \$45 in 26 weeks.

b) How much is the investment worth?

$$A = P + I$$

$$= 2000 + 45$$

$$= \$2045$$

**The Simple Interest Triangle → Finding P, r, and t**

Rearrange the simple interest formula to find the principal, interest rate, and time.

$I = Prt$



$P = \frac{I}{rt}$

$r = \frac{I}{Pt}$

$t = \frac{I}{Pr}$

**EXAMPLE 2**

How much principal is needed to earn \$500 in interest in 2 years invested at 2.5% simple interest?

$$I = \$500$$

$$P = ?$$

$$r = 2.5\% = 0.025$$

$$t = 2 \text{ years}$$

$$P = \frac{I}{rt}$$

$$= \frac{500}{0.025(2)}$$

$$= 10000$$

∴ You need to invest \$10,000

**EXAMPLE 3**

What rate of simple interest is needed to get \$7 000 to grow to \$10 000 in 5 years?

$$I = 10000 - 7000 = 3000$$

$$P = 7000$$

$$r = ?$$

$$t = 5 \text{ years}$$

$$r = \frac{I}{Pt} = \frac{3000}{7000 \cdot 5} = 0.086 \rightarrow \text{multiply it by } 100 \rightarrow 8.6\%$$

∴ The interest rate needs to be 8.6%

**EXAMPLE 4**

How long would it take \$1 500 to grow to \$2 000 at a simple interest rate of 3%?

$$I = 2000 - 1500 = 500$$

$$P = 1500$$

$$r = 3\% = 0.03$$

$$t = ?$$

$$t = \frac{I}{Pr} = \frac{500}{1500(0.03)} = 11.11$$

∴ It would take approximately 11.11 years.