Chapter 4: Exponential Functions

Reviewing the Exponent Laws

 a^{m} is a power in exponential form where: m is the exponent

a is the base m is

m is a power of base a

In expanded form, $a^m = a \times a \times a \times a \times a \dots$ (multiply a by itself as many times as given by the value of m, exponent)

To **simplify** an expression means to leave the final answer in exponential form.]

RULE	EXAN	MPLE	PRACTICE
1) MULTIPLICATION of POWERS keep the base, add the exponents.	$a^2 \times a^5 = a^7$		Simplify $(2a^2b^3)(-3a^4b^6)$ = $(2)(-3)(a^2)(a^4)(b^3)(b^6)$ = $-6a^{2+4}_4b^{3+4}_5$
2) DIVISION of POWERS keep the base, subtract the exponents.	$a^5 \div a^2 = a^3$		Simplify $\frac{27x^9}{3x^{-6}} = 9x^{9-(-6)}$ = $9x^{9+6}$ = $9x^{15}$
3) POWER of a POWER keep the base, multiply the exponents.	$(a^2)^5 = a^{10}$		Simplify $(a^{-2})^{-3} \times 3a^{6}$ $= a^{-2 \cdot -3} \times 3a^{6}$ $= 1 \cdot a \times 3a^{6}$ $= 3a^{6+1} \longrightarrow = 3a^{12}$
4) POWER of a PRODUCT distribute the exponent over the brackets to each term inside. Then apply rule #3	$(2a^{3}b^{2})^{4} = (2^{1})^{4}(a^{3})^{4}(b^{2})^{4}$ $= (2^{1\times4})(a^{3\times4})(b^{2\times4})$ $= 2^{4}a^{12}b^{8}$ $= 16a^{12}b^{8}$		Simplify $(-2a^2b^5)^3$ = $(-2)^3 \cdot (a^2)^3 \cdot (b^5)^3$ = $-8 \cdot a^{2\times 3} \cdot b^{5\times 3}$ = $-8a^6b^{15}$
5) POWER of a QUOTIENT same as rule #4	$\left(\frac{a^3}{b^2}\right)^3 = \frac{(a^3)^3}{(b^2)^3}$ $= \frac{a^{3\times 3}}{b^{2\times 3}}$ $= \frac{a^9}{b^6}$		Simplify $(\frac{12x^5}{4y^3})^3$ $= (\frac{3x^5}{9^3})^3$ $= \frac{(3)^3(x^5)^3}{(9^2)^3}$ $= \frac{27x^{15}}{9^4}$
6) NEGATIVE EXPONENT reciprocate the base, switch the sign of the exponent	$a^{-2} = \frac{1}{a^2}$	$\left(\frac{2}{3}\right)^{-2} = \left(\frac{3}{2}\right)^2$ $= 9/4$	Simplify $(\frac{2x^3}{3y^2})^{-3}$ $= (\frac{3y^2}{2x^3})^3$ $= \frac{(3)^3(y^2)^3}{(2)^3(x^2)^3}$ $= \frac{27y^6}{8x^9}$
7) ZERO EXPONENT depending on the sign of the base, it is either equal to 1 or -1	$x^0 = 1$	$-x^0 = -1$	Simplify $-(\underline{14a^3b^{-4}})^0$ $=\underline{-1}$

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Ex1. Use the exponent laws to simplify the following. (Remember more than one law can be used to simplify an expression completely.)

a.
$$(4ab^{4})(-5a^{3}b^{2})$$

= $(4)(-5)(a)(a^{3})(b^{4})(b^{2})$
= $-20a^{1+3} \cdot b^{4+2}$
= $-20a^{4}b^{6}$

$$c. \left(-\frac{1}{2}c^{2}d^{3}\right)^{4}$$

$$= \left(-\frac{1}{2}\right)^{4} \left(c^{2}\right)^{4} \left(d^{3}\right)^{4}$$

$$= \frac{1}{16}c^{2}d^{3}d^{3}$$

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b.
$$(12b^{2})(8b^{4}) \div (6b^{-10})$$

$$= (12)(8)b^{2+14} \div 6b^{-10}$$

$$= 96b^{-2} \div 6b^{-10}$$

$$= 16b^{-2-(-10)}$$

$$= 16b^{8}$$

$$d. \frac{(t^{7})^{3}(t)}{t^{16}} = \frac{1}{t^{16}}$$

$$= \frac{t^{21+1}}{t^{16}}$$

$$= t^{22-16}$$

$$= t^{6}$$

Ex2. Use the laws of exponents to simplify the following:

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a.
$$\frac{(-m^2n^3)^2(mn^{-4})}{(mn^3)^4} = \frac{(-1)^2(m^2)^2(n^3)^2(mn^{-4})}{(m)^4(n^3)^4}$$

$$= \frac{m^4 n^6 m n^{-4}}{m^4 n^{12}}$$

$$= \frac{m^5 n^2}{m^4 n^{12}}$$

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d.
$$\frac{(2^{-1}+4^{-2})}{(2^{-2}+4^{-1})} = \frac{3}{2} \frac{\frac{1}{2} + \frac{1}{16}}{\frac{1}{16}}$$

b.
$$\frac{x(x^{4a+1})}{x^{a+3}} = \frac{x^{1+4a+1}}{x^{a+3}}$$
$$= x^{2+4a-(a+3)}$$
$$= x^{2+4a-a-3}$$
$$= x^{3a-1}$$

$$= \frac{1}{\frac{1}{3}} \quad \text{reciprocate}$$

$$= \frac{3}{3}$$

$$d. \frac{(2^{-1}+4^{-2})}{(2^{-2}+4^{-1})} = \frac{\frac{8}{2} + \frac{1}{16}}{\frac{1}{4} + \frac{1}{4}}$$

$$= \frac{\frac{8+1}{16}}{\frac{1+1}{4}}$$

$$= \frac{\frac{9}{16}}{\frac{1}{16}} = \frac{9}{16}$$