

Task 1: The Distance Formula

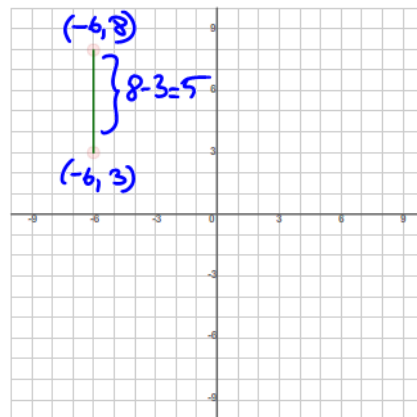
Vertical Line Segments

How long is the line segment on the graph?

5 units

How can the length be determined using a mathematical calculation instead of counting the number of squares?

Answer: 8-3=5



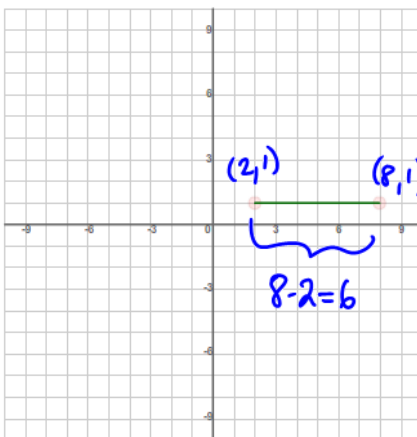
Horizontal Line Segments

How long is the line segment on the graph?

6 units

How can the length be determined using a mathematical calculation instead of counting the number of squares?

Answer: 8-2



Diagonal Line Segments

This line segment is more difficult to determine the length as the number of squares cannot be counted as they are on a diagonal.

First, calculate the vertical line segment

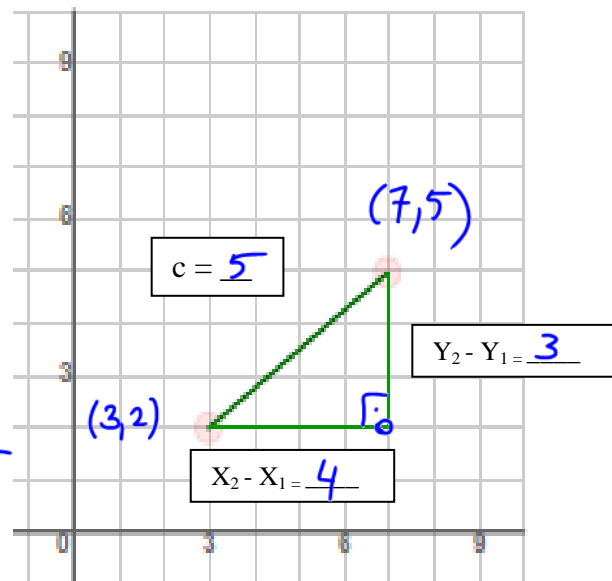
$$y_2 - y_1 = 5 - 2 = 3$$

Second, calculate the horizontal line segment

$$x_2 - x_1 = 7 - 3 = 4$$

Then, calculate the hypotenuse of the right triangle

$$\begin{aligned} c^2 &= a^2 + b^2 \\ &= 4^2 + 3^2 \rightarrow c^2 = \sqrt{(7-3)^2 + (5-2)^2} \\ &= 16 + 9 \\ \sqrt{c^2} &= 25 \\ c &= 5 \end{aligned}$$



Length of a Line Segment Formula:

$$\text{length} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Ex. Using the formula, find the length of the line segment \overline{DE} with $D(-3, 5)$ and $E(4, -6)$.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(4 - (-3))^2 + (-6 - 5)^2}$$

$$= \sqrt{(7)^2 + (-11)^2}$$

$$= \sqrt{49 + 121}$$

$$= \sqrt{170}$$

$$d = 13$$

\therefore The length is approx. 13

Task 2: Practice Complete the 5 practice examples in Discovering Distances.

Task 3: Applications

What types of triangles are there?

SCALEDNE = all sides unequal ISOSCELES = 2 equal sides

EQUILATERAL = 3 equal sides RIGHT-ANGLE TRIANGLE = follows the Pythagorean Theorem: $a^2 + b^2 = c^2$, where c is the hypotenuse (the longest side)

1. A triangle has these vertices: $D(6, 3)$, $O(-4, 1)$, $G(2, -5)$.

- Graph this triangle.
- Determine the length of each side using the formula.

Leave your answers with the square root.

$$\overline{DO} = \sqrt{(6 - (-4))^2 + (3 - 1)^2}$$

$$= \sqrt{(10)^2 + (2)^2}$$

$$= \sqrt{104}$$

$$= 2\sqrt{26}$$

$\overline{DO} = 2\sqrt{26}$

$$\overline{OG} = \sqrt{(-4 - 2)^2 + (1 - (-5))^2}$$

$$= \sqrt{36 + 36}$$

$$= \sqrt{72}$$

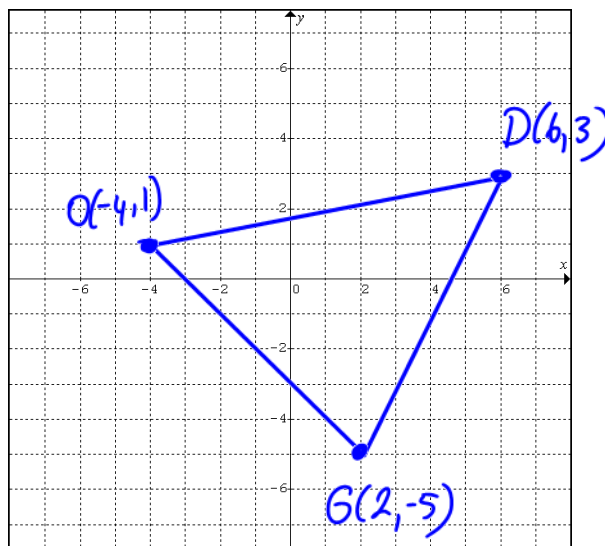
$\overline{OG} = 6\sqrt{2}$

$$\overline{DG} = \sqrt{(3 - (-5))^2 + (6 - 2)^2}$$

$$= \sqrt{64 + 16}$$

$$= \sqrt{80} = 4\sqrt{5}$$

$\overline{DG} = 4\sqrt{5}$

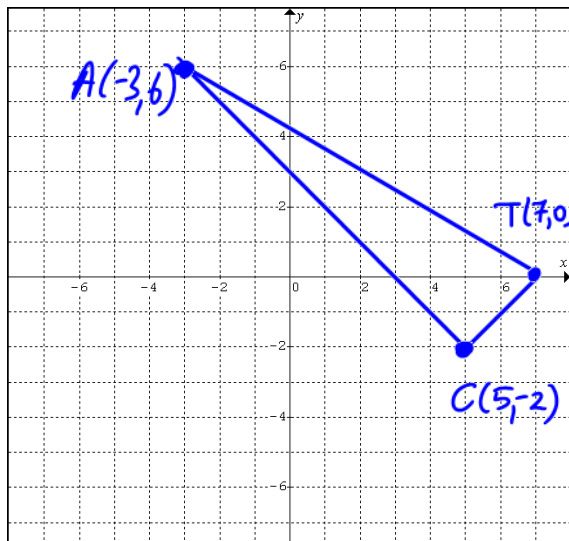


$\overline{DO} \neq \overline{OG} \neq \overline{DG}$

Therefore, $\triangle DOG$ is SCALEDNE (scalene, isosceles, or equilateral?)

2. A triangle has these vertices: C(5, -2), A(-3, 6), T(7, 0).

- a. Graph this triangle.
b. Use the formula to determine the length of each side. Leave your answers with the square root.



$$\begin{aligned} CA &= \sqrt{(-3-5)^2 + (6-(-2))^2} \\ &= \sqrt{64+64} \\ &= \sqrt{128} \quad \overline{CA} = 8\sqrt{2} \end{aligned}$$

$$\begin{aligned} AT &= \sqrt{(-3-7)^2 + (6-0)^2} \\ &= \sqrt{100+36} \quad \overline{AT} = 2\sqrt{34} \\ &= \sqrt{136} \end{aligned}$$

$$\begin{aligned} CT &= \sqrt{(5-7)^2 + (-2-0)^2} \\ &= \sqrt{4+4} \quad \overline{CT} = 2\sqrt{2} \\ &= \sqrt{8} \\ &= 2\sqrt{2} \end{aligned}$$

c. Therefore, $\triangle CAT$ is SCALED (scalene, isosceles, or equilateral?)

d. Use the three lengths and the Pythagorean Theorem to determine if $\triangle CAT$ is right angled.

$$\begin{array}{l|l} \text{LS} & \text{RS} \\ \hline (\sqrt{136})^2 & (\sqrt{128})^2 + (\sqrt{8})^2 \\ 136 & 128 + 8 \\ 136 = 136 & \end{array} \quad \text{LS} = \text{RS}, \text{ it's right angled}$$

e. Determine the slope of each side!

$$\begin{aligned} CA &= \frac{0-6}{5-(-3)} \\ &= \frac{-6}{8} \\ &= -\frac{3}{4} \\ &= -1 \end{aligned}$$

$$\begin{aligned} AT &= \frac{0-6}{7-(-3)} \\ &= \frac{-6}{10} \\ &= -\frac{3}{5} \end{aligned}$$

$$\begin{aligned} CT &= \frac{-2-0}{5-7} \\ &= \frac{-2}{-2} \\ &= 1 \end{aligned}$$

f. How can you use the slopes to determine whether $\triangle CAT$ is right angled?
if $m_{CA} \times m_{CT} = -1$, then $\triangle CAT$ is right angled.