

ARITHMETIC SERIES

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An **arithmetic series** is the sum of the terms in an arithmetic sequence.

For example, for the arithmetic sequence 1, 4, 7, 10, ... , **the arithmetic series** is $1 + 4 + 7 + 10 + \dots$ where t_4 represents the 4th term, S_4 represents the sum of the first 4 terms.

The sum of the first n terms of an arithmetic sequence (a series) can be calculated in two ways:

$$\textcircled{1} S_n = \frac{n[2a + (n-1)d]}{2}$$

$$\textcircled{2} S_n = \frac{n(t_1 + t_n)}{2}$$

Decide which one to use based on the information given.

Ex1. For the given arithmetic series, calculate t_{17} and S_{17} .

$$3 + 7 + 11 + \dots$$

Ex2. Find the sum of the first 12 terms of the arithmetic series with $a = 3$ and $t_{12} = 36$.

Ex3. Find the sum of the first 25 terms of the arithmetic series where the 14th term is 102 and terms decrease by 9.

Ex4. Calculate the sum of the arithmetic series.

$$-4 - 10 - 16 - \dots - 94$$

Ex5. In an amphitheatre, seats are arranged in 50 semicircular rows facing a domed stage. The first row contains 23 seats, and each row contains 4 more seats than the last. How many seats are there in total?

Ex6. Samantha deposited \$128 into her bank account. Each week, she deposits \$7 less than the previous week until she makes her last deposit of \$9. Find the total value of her deposits.