## SQUARE ROOTS \& PERFECT SQUARES

To understand square roots, first let's take a look at squares.
How to Square a Number: Just multiply it by itself.
Squares from $1^{2}$ to $12^{2}$

$$
\begin{aligned}
& 1 \text { Squared }=1^{2}=1 \times 1=1 \\
& 2 \text { Squared }=2^{2}=2 \times 2=4 \\
& 3 \text { Squared }=3^{2}=3 \times 3=9 \\
& 4 \text { Squared }=4^{2}=4 \times 4=16 \\
& 5 \text { Squared }=5^{2}=5 \times 5=25 \\
& 6 \text { Squared }=6^{2}=6 \times 6=36 \\
& 7 \text { Squared }=7^{2}=7 \times 7=49 \\
& 8 \text { Squared }=8^{2}=8 \times 8=64 \\
& 9 \text { Squared }=9^{2}=9 \times 9=81 \\
& 10 \text { Squared }=10^{2}=10 \times 10=100 \\
& 11 \text { Squared }=11^{2}=11 \times 11=121 \\
& 12 \text { Squared }=12^{2}=12 \times 12=144
\end{aligned}
$$

## PERFECT SQUARES

| 1 Squared $=1^{2}=1 \times 1=\mathbf{1}$ | $\begin{array}{llllllllllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 Squared $=2^{2}=2 \times 2=4$ | $\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 Squared $=3^{2}=3 \times 3=9$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 Squared $=4^{2}=4 \times 4=16$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 5 Squared $=5^{2}=5 \times 5=25$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6 Squared $=6^{2}=6 \times 6=36$ | $\begin{array}{lllllllllllll}\mathbf{5} & 5 & 10 & 15 & 20 & 25 & 30 & 35 & 40 & 45 & 50 & 55 & 60 \\ 6 & 6 & 12 & 18 & 24 & 30 & 30 & 42 & 48 & 54 & 60 & 66 & 72\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 7 Squared $=7^{2}=7 \times 7=49$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 7 Squared $=7^{2}=7 \times 7=49$ $8 \times 8 \quad 64$ | $7 \begin{array}{llllllllllllllllllllll}7 & 7 & 14 & 21 & 28 & 35 & 42 & 49 & 56 & 63 & 70 & 77 & 84\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 8 Squared $=8^{2}=8 \times 8$ | 8 |  |  |  |  |  |  |  |  |  |  |  |  |
| 9 Squared $=9^{2}=9 \times 9=81$ | $\begin{array}{llllllllllllllllll}9 & 9 & 18 & 27 & 36 & 45 & 54 & 63 & 72 & 81 & 90 & 99 & 108\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 10 Squared $=10^{2}=10 \times 10=100$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 11 Squared $=11^{2}=\|\|\times\|\|=12\|$ | $11 \begin{array}{llllllllllllll}11 & 11 & 22 & 33 & 44 & 55 & 66 & 77 & 88 & 99 & 110 & 121 & 132\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 12 Squared $=12^{2}=12 \times 12=144$ | $\begin{array}{lllllllllllll}12 & 12 & 24 & 36 & 48 & 60 & 72 & 84 & 96 & 108 & 120 & 13 & 144\end{array}$ |  |  |  |  |  |  |  |  |  |  |  |  |

## Square Roots:

A square root goes the other way:


3 squared is 9 , so a square root of 9 is 3
A square root of a number is a value that can be multiplied by itself to give the original number.
A square root of $\mathbf{9}$ is $\mathbf{3}$, because when $\mathbf{3}$ is multiplied by itself we get $\mathbf{9}$.
It is like asking "what can we multiply by itself to get this?"
The Square Root Symbol
$\sqrt{ }$ This is the special symbol that means "square root". It is called the radical.


## OPERATIONS WITH SQUARE ROOTS

Just follow the same BEDMAS rule when operating with fractions.
Simplify each expression:
a) $\sqrt{25}+\sqrt{16} \quad$ Read: Add the square roots of 25 and 16.
$=5+4$
$=9$
b) $\sqrt{3+6} \quad$ Read: Square root the sum of 3 and 6.
$=\sqrt{9}$
$=3$
c) $\sqrt{31+\sqrt{25}} \quad$ Read: Square root the sum of 31 and square root of 25 .
$\begin{aligned} & =\sqrt{31+5} \\ & =\sqrt{36}\end{aligned} \quad \rightarrow=6$
d) $\sqrt{\sqrt{169}+\sqrt{144}}$ Read: Square root the sum of square root of 169 and square root of 144 .
$=\sqrt{13+12} \quad \rightarrow=5$
$=\sqrt{25}$
e) $2 \sqrt{25} \quad$ Read: 2 times square root 25 .
$=2 \cdot(5)$
$=10$
f) $3 \sqrt{100}+2 \sqrt{16}$

$$
=3 \cdot(10)+2(4)
$$

$$
=30+8
$$

$$
=38
$$

$$
\begin{aligned}
& \text { g) } \sqrt{12-\sqrt{6+\sqrt{8+1}}} \text { from Right heft } \\
= & \sqrt{12-\sqrt{6+\sqrt{9}}} \\
= & \sqrt{12-\sqrt{6+3}} \\
= & \sqrt{12-\sqrt{9}} \\
= & \sqrt{12-3} \\
= & \sqrt{9}
\end{aligned}
$$

