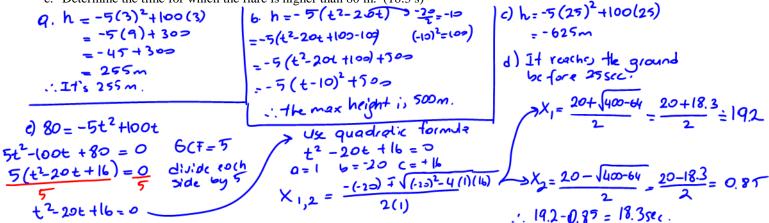
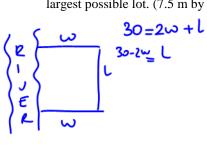
diapter of Quadratic Equation

- 1. An equation representing the height of a flare, h metres, above the release position, after t seconds, is $h = -5t^2 + 100t$. a. What is the height of the flare after 3 s? (255 m)
- b. What is the maximum height reached by the flare? (500 m)
- c. What is the height of the flare after 25 s? (-625 m)
- d. Does your answer in part c make sense? Explain. (No . . .)
- e. Determine the time for which the flare is higher than 80 m. (18.3 s)

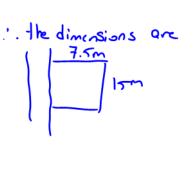


- 2. When a flare is fired vertically upward, its height, h metres, after t seconds is modelled by the equation $h = -5t^2 + 153.2t$.
- a. Is the flare on the ground or on a stand? (ground)
- b. How long is the flare in the air? (30.64 sec)
- c. What is the maximum height of the flare? (1173.5 m)
- d. For how many seconds is the flare higher than 1 km. (11.78 s)

3. A rectangular lot is bounded on one side by a river and on the other three sides by a total of 30 m of fencing. A formula that represents the area of the lot, A square metres, in terms of its width, x metres, is $A = 30x - 2x^2$. Calculate the dimensions of the largest possible lot. (7.5 m by π m)



$$A=\omega(30-2\omega)$$
= 30 \omega-2\omega^2 + 30 \omega
= -2(\omega^2 - 15\omega) \frac{-15}{2} \left(15\delta^2 - 56.25 \right)
= -2(\omega^2 - 15\omega + 56.25 - 66.25 \right)
= -2(\omega^2 - 15\omega + 56.25 \right) + 112.5
= -2(\omega - 7.5)^2 + 112.5



MPM2D1

Day 9: The Quadratic Equation APPLICATIONS

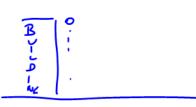
Date: _____ Chapter 6: Ouadratic Equations

4. A ball is dropped over the roof of a building. The equation to model this scenario is: the height of the building in feet after *t* seconds.

 $h = -16t^2 + 75$, where h is

a. How high is the building? (75 ft)

b. How long does it take the ball to land? (sec)



a),
$$h = -16t^2 + 75$$
 sub "0" for "t = -16(0)²+75 = 75ft.

b.) Solve the equation
$$O = -16t^2 + 75 \text{ move}^{-16t^2} + 5 \text{ ts}^{-16t^2} + 5 \text{$$

5. The power, P watts, supplied to a circuit by a 9-V battery is given by the formula $P = 9I - 0.5I^2$, where I is the current in amperes. What is the maximum power? (40.5 W)

$$P = -0.5I^{2} + 9I$$

$$= -0.5(I^{2} - 18I)^{3} - 18/2 = -9 (-9)^{2} = 8I$$

$$= -0.5(I^{2} - 18I + 8I - 8I)$$

$$= -0.5(I^{2} - 18I + 8I) + 40.5$$

$$= -0.5(I - 9)^{2} + 40.5$$
Vertey is $(9, 40.5)$; therefore the max power is 40.5 w

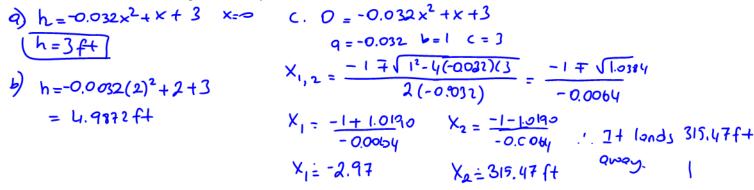
6. Computer software programs are sold to students for \$20 each. Three hundred students are willing to buy them at this price. For every \$5 increase in price, there are 30 fewer students willing to buy the software. A formula that represents the revenue, R dollars, for an x dollar increase in price is $R = -6x^2 + 180x + 6000$. Calculate the selling price that will produce the maximum revenue. What is the maximum revenue? (\$35, \$7350)

Revenue =
$$Price \times Amount$$

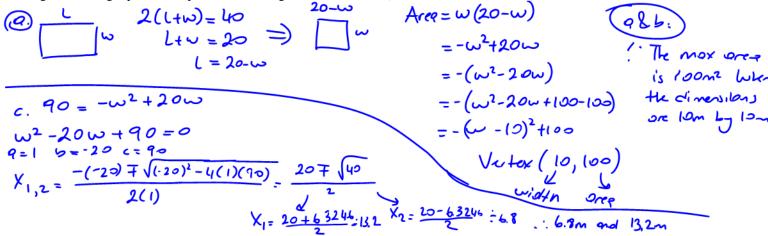
= $(20+5\times)(300-30\times)$
= $6000-600\times+1500\times-150\times^2$
 $R = -150\times^2+900\times+6000$
= $-150(\times^2-6\times)+6000$ = $-\frac{6}{2}=-3$ (-1)²=9
= $-150(\times^2-6\times+9-9)+6000$ | ... When you set the price to $20+5(3)=355$, you will $-150(\times^2-6\times+9)+1350+6000$ | max the rev. to \$7350
= $-150(\times-3)^2+7350$
... Vertex is $(3,7350)$
Price change

Date:

- 7. When a baseball is hit at a certain velocity and angle the height of the ball is given by the equation $h = -0.0032x^2 + x + 3$, where h is the height of the ball in feet, and x is the horizontal distance from home plate in feet.
- a. How high was the ball when it was hit? (3 ft)
- b. How high is the ball when it is 2 ft away from home plate? (4.98 ft)
- c. How far away from home plate does the ball land? (315.47 ft)
- d. What is the maximum height reached by the baseball? (81.125 ft)



- 8. Forty metres of fencing are available to enclose a rectangular pen. The area, A square metres, enclosed is given by $A = \frac{20x x^2}{x^2}$, where the length of the pen is x metres.
- e. What is the maximum area that can be enclosed? (100 m²)
- f. What are the dimensions of the pen with the maximum area? (10 m by 10 m)
- g. What length produces a pen with an area greater than 90 m²? (between 6.9 m and 13.1 m)



- 9. A company manufactures and sells designer T-shirts. The profit, P dollars, for selling a certain style of T-shirt is projected to be $P = -20x^2 + 1000x 6720$, where x dollars is the selling price of one T-shirt.
- a. What are the break even points? (\$8 and \$42) was ?= >
- b. What selling price gives the maximum profit? What is the maximum profit? (\$25, \$5780) $0 = -20 \times^{2} + 1000 \times -6720 \text{ G(F} = -20)$ $0 = -20 \left(\times^{2} 50 \times + 336 \right) \text{ divide each side}$ $-20 \left(\times^{2} 50 \times + 336 \right) \text{ divide each side}$ $0 = \times^{2} 50 \times + 336$ $0 = \times^{2} 50 \times + 336$ $0 = 1 \quad b = -50 \quad c = 336$ $0 = 1 \quad b = -50 \quad c = 336$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 6720$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 107$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 107$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 107$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 107$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 + 107$ $0 = -20 \left(\times^{2} 50 \times + 107 \right) + 125 \times 20 + 107$

Day 9: The Quadratic Equation APPLICATIONS

10. A life guard marks a rectangular swimming area at a beach with a 200 m rope. The width of the swimming area is x metres. The area enclosed is A square metres, where A = x(200 - 2x). What is the greatest area that can be enclosed? (5000 m²)



$$200 = 2\omega + L \qquad App = \omega (200 - 2\omega)$$

$$= -2\omega^{2} + 200\omega$$

$$= -2(\omega^{2} - 100\omega) - \frac{100 + 2 = -50}{(-50)^{2}} = 2500$$

$$= -2(\omega^{2} - 100\omega + 2500) + 5000$$

$$= -2(\omega^{2} - 100\omega + 2500) + 5000$$

$$= -2(\omega - 50)^{2} + 5000$$

$$= -2(\omega - 50)^{2$$

11. A company manufactures and sells novelty caps. The profit, P dollars, for selling a certain style of cap at t dollars each is projected to be $P = -15t^2 + 90t + 675$. What selling price is expected to give a maximum profit? What is the maximum profit? (\$3, \$810)

$$P = -15(t^{2} - 6t) + 675 - 6/2 = -3$$

$$= -15(t^{2} - 6t + 9 - 9) + 675$$

$$= -15(t^{2} - 6t + 9) + 135 + 675$$

$$= -15(t - 3)^{2} + 810$$

$$V(3, 8130) ... When the price is $3, the max profit is $810$$

12. A stone is thrown upward with an initial speed of 25 m/s. Its height, h metres, after t seconds is given by the equation $h = -5t^2 + 25t$. For how long is the stone higher than 30 m? (1 sec)

$$30 = -5t^{2} + 25t$$

$$0 = -5t^{2} + 25t - 30$$

$$0 = -5(t^{2} - 5t + 6)$$

$$0 = -5(t - 2)(t - 3)$$

$$t - 2 = 0$$

$$t = 2$$

$$3 - 2 = 156$$

