### MPM2D1 **Dav 9: The Ouadratic Equation APPLICATIONS**

- 1. An equation representing the height of a flare, h metres, above the release position, after t seconds, is  $h = -5t^2 + 100t$ .
- a. What is the height of the flare after 3 s? (255 m)
- b. What is the maximum height reached by the flare? (500 m)
- c. What is the height of the flare after 25 s? (-625 m)
- d. Does your answer in part c make sense? Explain. (No . . .)
- e. Determine the time for which the flare is higher than 80 m. (18.3 s)

- 2. When a flare is fired vertically upward, its height, h metres, after t seconds is modelled by the equation  $h = -5t^2 + 153.2t$ .
- a. Is the flare on the ground or on a stand? (ground)
- b. How long is the flare in the air? (30.64 sec)
- c. What is the maximum height of the flare? (1173.5 m)
- d. For how many seconds is the flare higher than 1 km. (11.78 s)
- $\begin{array}{c} 1 \text{ km. (11.76 s)} \\ 1 & \text{ C. We (an average 1 + 153.2t)} \\ 1 & \text{ He zeros} \end{array}$   $\begin{array}{c} 1 & 1 & 1000 = -5t^{2} + 153.2t \\ 1 & 1000 = -5t^{2} + 153.2t \\ 1 & 1000 = 0 \\ 1 & 5t^{2} 153.2t + 1000 = 0 \\ 1 & 5t^{2} 153.2t + 1000 = 0 \\ 1 & 9t^{2} 1000 = 0 \\ 1 & 9t^{2} 1000 = 0 \\ 1 & 9t^{2$ 9. Std form gives the y-int. h=-5t<sup>2</sup>+153.2t + 0 y.int = 0, it's on the ground. b. We need to find Z-Int. 0 - 5t2+153.2t GCF=-5+ 0 = -5t(t - 30.64) $|X_{1,2}| \xrightarrow{153.2 \mp 58.9}$ Vertex (15.32, 1173.5) t-30<u>.64 = 0</u> It= 30.  $|K_1 = \frac{153.2 + 58.7}{10} = 21.21$ 54=0 : It's in the air for 32.64 se. Y2= 153.2-58.9 = 9.43 12 · 2121-9.47= 11.785. it was above
  - 3. A rectangular lot is bounded on one side by a river and on the other three sides by a total of 30 m of fencing. A formula that represents the area of the lot, A square metres, in terms of its width, x metres, is  $A = 30x - 2x^2$ . Calculate the dimensions of the largest possible lot.  $(7.5 \text{ m by } \bigcirc \text{m})$

$$\begin{cases} 2 & 30 = 2\omega + 1 & A_{\pm}\omega(30 - 1\omega) \\ 30 = 2\omega + 1 & = 30 \omega - 2\omega^{2} & ... \text{ the dimensions } Qre \\ = 30 \omega - 2\omega^{2} & ... \text{ the dimensions } Qre \\ = -2\omega^{2} + 30\omega & ... \text{ the dimensions } Qre \\ = -2(\omega^{2} - 15\omega) - \frac{15}{2}(15)^{2} - 56.25 & ... \text{ the dimensions } Qre \\ = -2(\omega^{2} - 15\omega) - \frac{15}{2}(15)^{2} - 56.25 & ... \text{ the dimensions } Qre \\ = -2(\omega^{2} - 15\omega + 56.25 - 66.71) \\ = -2(\omega^{2} - 15\omega + 56.25) + 112.5 \\ = -2(\omega - 7.5)^{2} + 112.5 \end{cases}$$

MPM2D1Date:Day 9: The Quadratic Equation APPLICATIONSChapter 6: Quadratic Equations4. A ball is dropped over the roof of a building. The equation to model this scenario is:  
the height of the building? (75 ft)
$$h = -16t^2 + 75$$
, where h isb. How long does it take the ball to land? $= sec$ B  
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 $\downarrow$  $= -16(c0)^2 + 75$ B  
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 $\downarrow$  $= -16(c0)^2 + 75$  $g$   
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 $\downarrow$  $h = -16t^2 + 75$  move $R$   
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 $\downarrow$  $h = -16t^2 + 75$  move $R$   
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 $\downarrow$  $h = -16t^2 + 75$  move $R$   
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 $\downarrow$  $h = -16t^2 + 75$  $R$   
 $\downarrow$  $h = -16t^2 + 75$ <

5. The power, *P* watts, supplied to a circuit by a 9-V battery is given by the formula  $P = 9I - 0.5I^2$ , where *I* is the current in amperes. What is the maximum power? (40.5 W)

$$\begin{aligned} \mathcal{P} &= -0.5 \mathbf{I}^{2} + 9\mathbf{I} \\ &= -0.5 \left( \mathbf{I}^{2} - 18\mathbf{I} \right)^{-18/2} = -9 \quad (-9)^{2} = 8\mathbf{I} \\ &= -0.5 \left( \mathbf{I}^{2} - (8\mathbf{I} + 8\mathbf{I} - 8\mathbf{I} \right) \\ &= -0.5 \left( \mathbf{I}^{2} - (8\mathbf{I} + 8\mathbf{I} \right) + 40.5 \\ &= -0.5 \left( \mathbf{I} - 9 \right)^{2} + 40.5 \end{aligned}$$

$$V_{c} + c_{Y} \quad is \quad (9, 40.5); \text{ therefor the max power is 40.5 w}$$

6. Computer software programs are sold to students for \$20 each. Three hundred students are willing to buy them at this price. For every \$5 increase in price, there are 30 fewer students willing to buy the software. A formula that represents the revenue, R dollars, for an x dollar increase in price is  $R = -6x^2 + 180x + 6000$ . Calculate the selling price that will produce the maximum revenue. What is the maximum revenue? (\$35, \$7350)

$$Revenue = Price \times Amount
= (20+5x)(300-30x)
= 6000-600x+1500x-150x2
R = -150x2+900x+6000
= -150(x2-6x)+6000 -6 = -3 (-1)2=9
= -150(x2-6x)+9 + 1350+6000 -7 (-6 = -3) (-1)2=9
= -150(x2-6x)+9 + 1350+6000 -7 (-6 = -3) (-1)2=9
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= -150(x2-6x)+9 + 1350+6000 -7 (-6 = -3) (-7)2=9
= -150(x2-3)2+7350 -7 (-7)2=9$$

### MPM2D1 Day 9: The Ouadratic Equation APPLICATIONS

### Date: \_\_\_\_\_ Chapter 6: Quadratic Equations

- 7. When a baseball is hit at a certain velocity and angle the height of the ball is given by the equation  $h = -0.0032x^2 + x + 3$ , where *h* is the height of the ball in feet, and *x* is the horizontal distance from home plate in feet.
- a. How high was the ball when it was hit? (3 ft)
- b. How high is the ball when it is 2 ft away from home plate? (4.98 ft)
- c. How far away from home plate does the ball land? (315.47 ft)
- d. What is the maximum height reached by the baseball? (81.125 ft)

a) 
$$h = -0.032 \times^2 + \times + 3 \times = 0$$
  
(h = 3 ft)  
b)  $h = -0.032 \times^2 + 2 + 3$   
= 4.9372 ft  
 $X_{1,2} = \frac{-1 \mp \sqrt{1^2 - 4(-0.032)(3)}}{2(-0.032)} = \frac{-1 \mp \sqrt{1.0384}}{-0.0064}$   
 $X_{1,2} = \frac{-1 \mp \sqrt{1^2 - 4(-0.032)(3)}}{2(-0.032)} = \frac{-1 \mp \sqrt{1.0384}}{-0.0064}$   
 $X_{1,2} = \frac{-1 \pm 1.0190}{2(-0.0054)} \times 2 = \frac{-1 \pm \sqrt{1.0384}}{-0.0064}$   
 $X_{1} = -\frac{1 \pm 1.0190}{-0.00654} \times 2 = \frac{-1 \pm 1.0190}{-0.0064}$   
 $X_{1} = -\frac{1 \pm 1.0190}{-0.00654} \times 2 = \frac{-1 \pm 1.0190}{-0.0064}$   
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- 8. Forty metres of fencing are available to enclose a rectangular pen. The area, A square metres, enclosed is given by  $A = \frac{26x x^2}{x^2}$ , where the length of the pen is x metres.
- e. What is the maximum area that can be enclosed?  $(100 \text{ m}^2)$
- f. What are the dimensions of the pen with the maximum area? (10 m by 10 m)
- g. What length produces a pen with an area greater than 90 m<sup>2</sup>? (between 6.9 m and 13.1 m)



- 9. A company manufactures and sells designer T-shirts. The profit, *P* dollars, for selling a certain style of T-shirt is projected to be  $P = -20x^2 + 1000x 6720$ , where *x* dollars is the selling price of one T-shirt.
- a. What are the break even points? (\$8 and \$42)
- b. What selling price gives the maximum profit? What is the maximum profit? (\$25, \$5780)

## MPM2D1 Day 9: The Quadratic Equation APPLICATIONS

# Date: \_\_\_\_\_ Chapter 6: Quadratic Equations

10. A life guard marks a rectangular swimming area at a beach with a 200 m rope. The width of the swimming area is x metres. The area enclosed is A square metres, where A = x(200 - 2x). What is the greatest area that can be enclosed? (5000 m<sup>2</sup>)

11. A company manufactures and sells novelty caps. The profit, *P* dollars, for selling a certain style of cap at *t* dollars each is projected to be  $P = -15t^2 + 90t + 675$ . What selling price is expected to give a maximum profit? What is the maximum profit? (\$3, \$810)

12. A stone is thrown upward with an initial speed of 25 m/s. Its height, h metres, after t seconds is given by the equation  $h = -5t^2 + 25t$ . For how long is the stone higher than 30 m? (1 sec)