$\qquad$

We can now solve a quadratic equation by graphing, factoring, completing the square or the quadratic
formula. We need to know how to apply these skills and use the most appropriate method in a given situation.

## Example 1: Path of an Object

The formula $h=-\frac{1}{2} g t^{2}+v_{o} t+h_{o}$ can be used to model the height of a projectile, where $g$ is acceleration due to gravity, which is $9.8 \mathrm{~m} / \mathrm{s}^{2}$ on Earth, $\mathrm{v}_{0}$ is the initial vertical velocity, in metres per second, and $\mathrm{h}_{\mathrm{V}}$ is the initial height, in metres.
a. Create a model for the height of a toy rocket launched upward at $60 \mathrm{~m} / \mathrm{s}$ from the top of 3-n platform.

$$
\begin{aligned}
& h=-\frac{1}{2}(9.8) t^{2}+60 t+3 \\
& h=-4.9 t^{2}+60+3
\end{aligned}
$$

b. How long would the rocket take to fall to Earth, rounded to the nearest hundredth of a second?

$$
\begin{aligned}
& \begin{array}{l}
0=-4.9 t^{2}+6 a+3 \\
a=-4.9 \quad b=60 \quad c=3 \\
x_{1,2}
\end{array}=\frac{-b \mp \sqrt{b^{2}-49 c}}{2 q}=\frac{-60 \mp \sqrt{(60)^{2}-4(-4.9)(3)}}{2(-4.9)}=\frac{-60 \mp \sqrt{3600+58.8}}{-9.8}=\frac{-60 \mp \sqrt{3658.8}}{-9.8} \\
& x_{1,2}=\frac{-60 \mp 60.5}{-9.8} \longrightarrow x_{1}=\frac{-60+60.5}{-9.8}=-0.05 \\
& \quad x_{2}=\frac{-60-60.5}{-9.8}=12.3 \quad \text { for the rocket to foll to Earth. }
\end{aligned}
$$

c. What is the maximum height of the rocket, rounded to the nearest metre?

$$
\begin{aligned}
h & =-4.9 t^{2}+60 t+3 \\
& =-4.9\left(t^{2}-12.24 t\right)+3 \quad \frac{-12.24}{2}=-6.12 \quad(-6.12)^{2}=37.45 \\
& =-4.9\left(t^{2}-12.24 t+37.45-37.45\right)+3 \\
& =-4.9\left(t^{2}-12.24 t+37.45\right)+183.5+3 \\
& =-4.9(t-6.12)+186.5
\end{aligned}
$$

$$
\therefore \text { about } 187 \mathrm{~m}
$$

d. Over what time interval is the height of the toy rocket greater than 150 m ? Round to the nearest hundredth of a second.

$\qquad$

## Day 8: The Quadratic Formula APPLICATIONS

## Example 2: Consecutive Numbers

The product of two consecutive even numbers is 5624 . What are the numbers?

$$
\begin{aligned}
& \text { Let " } x \text { " be one even number, therefore } x+2 \text { is the next ore. } \\
& \left.\begin{array}{l}
x(x+2)=5624 \\
x^{2}+2 x=5624 \\
x^{2}+2 x-5624=0 \\
a=1 \quad b=2 \quad c=-5624
\end{array}\right\} \begin{array}{l}
x_{1,2}=\frac{-b \mp \sqrt{b^{2}-4 a c}}{2 a}=\frac{-2 \mp \sqrt{2^{2}-4(1)(-5624)}}{2(1)}=\frac{-2 \mp \sqrt{22500}}{2} \\
=\frac{-2 \mp 150}{2}
\end{array} \quad \begin{array}{l}
x_{1}=\frac{-2+150}{2}=74 \\
x_{2}=\frac{-2-150}{2}=-76
\end{array}
\end{aligned}
$$

$\therefore$ The numbers ore either 74,76 or $-76,-74 \vee$

## Example 3: Width of a Path

A rectangular park measures 100 m by 60 m . A path of constant width is to be paved around the perimeter. The mayor wants to be sure that the path does not reduce the area of the grass by more than $10 \%$. What is the maximum allowable width of the path, rounded to the nearest tenth of a metre?

$$
90 \% \text { of the area of the oort }=6000 \times 90 \%=5400
$$


$\left.100 \quad \begin{array}{l}5400=(60-2 x)(100-2 x) \\ 5400=6000-120 x-200 x+4 x^{2} \\ 0=4 x^{2}-320 x+600 \\ \frac{0}{4}=\frac{4\left(x^{2}-80 x+150\right)}{4} \\ 0=x^{2}-80 x+150\end{array}\right\}=\frac{80 \mp 76.2}{2} \frac{b=-8 \quad c=150}{29}=\frac{80 \mp \sqrt{640-4(1)(150)}}{2}=\frac{8 \mp \sqrt{5800}}{2}$

## Example 4: Right Triangle

One leg of a right triangle is 1 cm longer than the other leg. The length of the hypotenuse is 9 cm greater than that of the shorter leg. Find the length of the three sides.


